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# LHC INTERACTION REGION CORRECTION SCHEME STUDIES\*

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#### Abstract

In a companion paper we showed that the performance of the Large Hadron Collider (LHC) at collision energy is limited by the field quality of the interaction region quadrupoles and dipoles. In this situation, the dynamic aperture can be increased through local multipole correctors. Since the betatron phase advance is well defined for magnets that are located in regions of large beta functions, local corrections can be very effective and robust. We compare possible compensation schemes and propose a corrector layout to meet the required dynamic aperture performance.

#### 1 INTRODUCTION

In the LHC the field errors of the FNAL and KEK triplet quadrupoles are a leading source of the dynamic aperture reduction at collision [1]. Local interaction region correctors are thus proposed to reach the LHC target dynamic aperture of 12 times the transverse rms beam size  $(12\sigma_{xy})$ .

During the past two years of magnet proto-type manufacturing, testing, and field quality analysis of the US-LHC magnets, there has been several iterations of the magnet design that leads to improvement of the field quality. Accordingly, there has been several iterations of the proposed compensation schemes for the IR region [2, 3]. First, bodyend compensation of the systematic  $b_6$  is not planned due to the reduced  $b_6$  in the lead end and the uncertainty in  $b_6$  measurement. Then, magnetic tuning shims are no longer planned due to the reduction of the random  $b_3$  and  $b_4$  errors and mechanical complications associated with shimming. Finally, the corrector layout and strength requirements are modified after CERN's decision have the Q1 and Q3 quadrupoles built by KEK, and to have the Q2A and Q2B quadrupoles built by FNAL.

Fig. 1 shows the tentative location of the proposed correctors assumed for this study. We choose the corrector strenght such that the action angle kick accross the interaction region is minimized [4]. For this, two correctors per order and interaction region are needed. An accurate measurement of the multipole errors in the quadrupoles is necessary. A local correction scheme like this does not prevent the implementation of global correction schemes proposed in references [5, 6] in the future. During the workshop, it became clear that as the systematic  $b_{10}$  in the body of KEKbuilt quadrupoles is further reduced, it is neither necessary

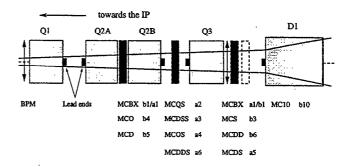


Figure 1: Tentative layout of the LHC inner triplet region assumed for the study of this paper.

nor desirable to plan for any  $b_{10}$  correctors. On the other hand, due to strength requirements for the  $b_6$  correction, fewer layers of correction elements should be designed in the corrector package that contains the  $b_6$  element. Fig. 2 shows the final proposed layout from the workshop [7].

In Sec. 2 the correction algorithm is presented in short. In the following section the effectiveness of four correction schemes is evaluated with element-by-element particle tracking over 1,000 turns. Only IP1 and IP5 are corrected in these studies.

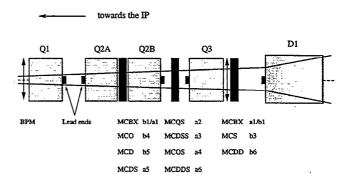


Figure 2: Final proposed layout of the LHC inner triplet region from this Workshop.

#### 2 IR COMPENSATION SCHEMES

The error compensation is based on the minimization of action-angle kicks [4] produced by each multipole error  $b_n$  (or  $a_n$ ) over a pair of inner triplets. Using two correction elements of each multipole order  $c_n$  (either  $a_n$  or  $b_n$ ), we

<sup>\*</sup> Work performed under the auspices of the US Department of Energy.

minimize the sum

$$\int_{L} dl C_{z} B_{0} c_{n} + (-)^{n} \int_{R} dl C_{z} B_{0} c_{n}, \quad z = x, y \quad (1)$$

taking advantage of the negligible betatron phase advance within each triplet and D1, and approximate the phase advance between the triplets by  $180^{\circ}$ . The integral is over the entire left-hand-side (L) or right-hand-side (R) MQX triplet and D1. In dipoles  $B_0$  is simply the main field, in quadrupoles it is the field at the reference radius  $R_{ref}$ . In general, the weights  $C_z$  in Eq. 1 are chosen according to the multipoles as:

	even b <sub>n</sub>	odd $b_n$	even a <sub>n</sub>	odd a <sub>n</sub>
$\overline{C_x}$	$\beta_x^{n/2}$	$eta_x^{n/2}$	$\beta_x^{(n-1)/2}\beta_y^{1/2}$	$\overline{eta_x^{(n-1)/2}eta_y^{1/2}}$
$C_{m{y}}$	$\beta_y^{n/2}$	$\beta_x^{1/2}\beta_y^{(n-1)/2}$	$\beta_x^{1/2}\beta_y^{(n-1)/2}$	$\beta_y^{n/2}$

The compensation is equally effective for both intersecting beams, since the optics of the interaction region is antisymmetric. However, it does not take into account the closed-orbit deviation due to the crossing angle, and the fact that the crossing planes are respectively vertical and horizontal in the two high luminosity interaction points. On the other hand, the effect of this closed orbit feeddown is partially compensated by the feeddown from the correctors.

## 3 CORRECTION SCHEME COMPARISON

There are three corrector packages (MCX1, MCX2, MCX3) in each triplet (see Fig. 1 and Fig. 2). Each MCX1 and MCX3 contains two dipole layers, and each MCX2 contains a skew quadrupole layer. A straightforward approach (scheme 1, see Tab. 1) is to have 3 additional layers of nonlinear skew multipoles  $(a_3, a_4, a_6)$  for MCX2, and two additional layers of nonlinear multipoles for MCX1 and MCX3. These layers could be a combination of any of  $b_3$ ,  $b_4$ ,  $b_5$  and  $b_6$  layers. For each multipole, two correction elements, located symmetrically at both sides of the IP, can be activated to minimize the kick in both the x and y directions (compare Eq. 1). Due to the lattice symmetry both beams are corrected.

Scheme 1 increases the dynamic aperture by 38% in the unmixed and 28% in the mixed case. With an additional  $a_5$  corrector (scheme 2) the improvement is 42% and 32% respectively. A further improvement can be achieved using a  $b_{10}$  corrector, as shown in Tab. 2. However, a  $b_{10}$  corrector is difficult to built is not needed with the KEK multipole error table version 3.0 [1].

Fig. 3 depicts the effect of correction scheme 4 on the tune space. The tune spread of particles with transverse amplitudes up to 6 times the rms beam size is reduced from more than  $4 \times 10^{-3}$  to about  $7 \times 10^{-4}$ .

We also investigated the effect of misalignment of the corrector layers. With an rms misalignment of 0.5mm in

Table 1: Interaction region correction schemes. Only the non-linear correctors are shown.

	MCX1	MCX2	MCX3	remark
scheme 1	2 layers	3 layers	2 layers	
	$b_4, b_5$	$a_3, a_4, a_6$	$b_3, b_6$	
scheme 2	3 layers	3 layers	2 layers	
	$b_3, b_5, b_6$	$a_3, a_4, a_6$	$b_4, a_5$	
scheme 3	2 layers	3 layers	2 layers	scheme 1
	$b_4, b_5$	$a_3, a_4, a_6$	$b_3, b_6$	$+ b_{10}$
scheme 4	3 layers	3 layers	2 layers	scheme 2
	$b_3, b_5, b_6$	$a_3, a_4, a_6$	$b_4, a_5$	$+ b_{10}$

Table 2: Comparison of local IR corrector effectiveness assuming that the interaction region quadrupole errors are measured to a 5% rms accuracy. The dynamic aperture (DA) is given in units of  $\sigma_{xy}$ . The physical aperture of 60 mm corresponds to about  $14\sigma_{xy}$ .

Case	DA mean	DA rms	DA min
UNMIXED:			
no correction	8.5	1.4	7
scheme 1	11.8	2.4	8
scheme 2	12.1	2.2	9
scheme 3	15.4	1.8	12
scheme 4	15.9	1.7	13
MIXED:			
no correction	10.0	1.5	8
scheme 1	12.8	1.1	10
scheme 2	13.2	1.3	11
scheme 3	16.1	1.8	13
scheme 4	17.6	1.6	14

the horizontal and vertical planes we find no degradation of the dynamic aperture(see Tab. 3).

Table 3: Effect of corrector displacement. The dynamic aperture (DA) is given in units of  $\sigma_{xy}$ .

Case	DA mean	DA rms	DA min
MIXED scheme 4	17.6	1.6	14
MCX1-3 displaced with 0.5 mm rms	17.8	1.3	15

The required strength of the multipole correctors can be provided by 50cm long spool pieces wound using the LHC sextupole corrector wire and operating at less than 50% margin at 600A [8]. At IP2, the IR correctors are also designed to reduce the effect of the D1 errors during low- $\beta$  heavy ion operations [9]. We computed the maximum corrector strength order by order out of a distribution of 80 values (systematic multipole error with positive and negative sign  $\times$  10 random error seeds  $\times$  2 interaction regions  $\times$  2

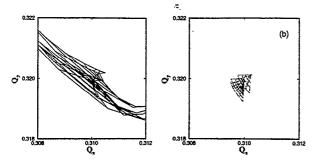
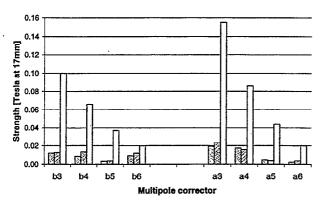


Figure 3: Effect of IR multipole correction on the covered tune space. (a) shows the uncorrected machine and (b) the corrected machine with scheme 4.

correctors per interaction region). The result for correction scheme 2 is shown in Fig. 4 for the KEK multipole error tables version 2.0 and 3.0 (both together with the FNAL multipole error table version 2.0). The available correction strength is sufficient for all orders of multipole errors.



☐ KEK V2.0 FNAL V2.0 ☐ KEK V3.0 FNAL V2.0 ☐ Maximum available

Figure 4: Available and needed corrector strength for scheme 2. The needed corrector strength shows the maximum out of a distribution of 20 machines with two correctors each at IP1 and IP5.

#### 4 SUMMARY

Local nonlinear interaction region correctors, up to multipole order 6, are proposed for compensating the interaction quadrupole errors. These correctors can improve the dynamic aperture by  $2-3\sigma_{xy}$ . The required correction strength is well within the available strength.

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### 5 REFERENCES

[1] W. Fischer et al., "LHC interaction region quadrupole error impact studies", these proceedings.

- [2] J. Wei et al., "US-LHC IR magnet error analysis and compensation", EPAC 1998 proceedings (1998) p. 380.
- [3] J. Wei et al., "Interaction region local correction for the Large Hadron Collider", PAC 1999 proceedings (1999) p. 2921.
- [4] J. Wei, "Principle of interaction region local correction", these proceedings.
- [5] T. Sen et al., "Correction schemes for the LHC lattice at collision", these proceedings.
- [6] J. Shi, "Global correction of magnetic field errors in LHC interaction regions", these proceedings.
- [7] J. Wei, J. Strait, J.-P. Koutchouk, T. Taylor, "Summaries", these proceedings.
- [8] M. Karppinen, private communications.
- [9] V. Ptitsin, W. Fischer and J. Wei, "LHC interaction region correction in heavy ion operation", these proceedings.

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